We derive the weak formulation of the Navier-Stokes equations directly from the basic physical principles, showing that the weak formulation and thus also the weak solution are completely natural for this system. Next, we will show the effect of various boundary conditions on this weak formulation. Finally, we summarize the already known concepts of solutions of the Navier-Stokes equations with theorems about their existence and explain relationships among them.